

Mathematical Method of Physics

Problem 6

- 6.1 Solve the following wave equation with damping proportional to velocity,

$$\frac{\partial^2 u(x, t)}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 u(x, t)}{\partial t^2} + \gamma \frac{\partial u(x, t)}{\partial t} ,$$

with the boundary conditions in the form

$$u(0, t) = u(L, t) = 0 ,$$

$$u(x, 0) = u_0 \sin \frac{\pi x}{L} ,$$

and the initial condition

$$\frac{\partial u(x, t)}{\partial t} \Big|_{t=0} = 0 .$$

- 6.2 Find the eigenfunctions and eigenenergies of a particle of mass m which is contained inside a cylinder of radius a and height L .
- 6.3 In a stationary state, the temperature distribution inside a sphere of radius a is described by the Laplace's equation. Solve it assuming that the surface of the sphere's top half is maintained at constant temperature T_0 , while the surface of its bottom half is kept at $T = 0$.